

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(END SEMESTER EXAMINATION)**

CLASS: BTECH  
BRANCH: EEE

SEMESTER : IV/ADD  
SESSION : SP/2025

**SUBJECT: EE305 DIGITAL SIGNAL PROCESSING**

TIME: 3 Hours

FULL MARKS: 50

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
  2. Attempt all questions.
  3. The missing data, if any, may be assumed suitably.
  4. Before attempting the question paper, be sure that you have got the correct question paper.
  5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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	[5]	CO	BL
Q.1(a) (i) Differentiate between time-invariant & time-variant system giving suitable examples.	[5]	1	2
(ii) Determine if the systems $y(n) = x(-n)$ is causal or non-causal.			
Q.1(b) Perform the (i) linear and (ii) circular convolution of the following two sequences. $x(n) = \{2, 1, 2, 4\}$ , $x(n) = \{1, 2, 3\}$ .	[5]	2	2
Q.2(a) (i) Derive the radix-2 Decimation in Time - Fast Fourier Transform (DIT-FFT) algorithm to calculate the DFT of a discrete time signal.	[5]	3	1
(ii) The first three points of the 4 point DFT of a real valued sequence are $\{6, 2+j2, -2\}$ . Determine the remaining one points.			
Q.2(b) Given a sequence $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$ , determine $X(k)$ using DIT-FFT algorithm.	[5]	3	3
Q.3(a) Explain frequency warping and causes of this effect.	[2]	4	2
Q.3(b) Obtain the transformation formula for the bilinear transformation.	[3]	4	3
Q.3(c) Determine $H(z)$ for a digital Butterworth IIR filter using impulse invariant transformation that satisfies the following constraint. Assume $T = 1$ Sec.	[5]	4	6
$\sqrt{0.5} \leq  H(e^{j\omega})  \leq 1, \quad 0 \leq \omega \leq \pi/2$ $ H(e^{j\omega})  \leq 0.2, \quad 3\pi/4 \leq \omega \leq \pi$			
Q.4(a) Define a linear phase filter. What conditions are to be satisfied by the impulse response of a FIR system in order to have a linear phase?	[5]	3,4	2,3,4
The transfer function of an FIR filter ( $M=7$ ) is $H(z) = \sum_{n=0}^{M-1} h(n)z^{-n}$ . Determine the magnitude response and show that the phase and group delays are constant.			
Q.4(b) The desired response of a low-pass filter is	[5]	3,4,5	3,4,5,6

$$H(e^{j\omega}) = \begin{cases} e^{-j3\omega}, & -\frac{3\pi}{4} \leq \omega \leq \frac{3\pi}{4} \\ 0, & \frac{3\pi}{4} < |\omega| \leq \pi \end{cases}$$

Determine and plot  $H(e^{j\omega})$  for  $M=7$  using Hamming window. Obtain the system function and construct the structure of filter.

- Q.5(a) Explain different type of architecture used in design of DSP processor with their advantages and disadvantages. [5] 5 4
- Q.5(b) (i) Describe the functionality of different components of DSP processor. What are the basic architectural features of DSP processors ? (ii) Given a 8 point sequence, find the percentage improvement in multiplication using DIT-FFT algorithm as compared to direct calculation of DFT using advanced digital signal processor. [5] 5 5

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