

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(MID SEMESTER EXAMINATION SP/2025)

CLASS: BTECH  
BRANCH: EEE

SEMESTER : IV/ADD  
SESSION : SP/2025

SUBJECT: EE305 DIGITAL SIGNAL PROCESSING

TIME: 02 Hours

FULL MARKS: 25

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- |   |     | CO   | BL   |
|---|-----|------|------|
| Q.1(a) Determine if the systems<br>(i) $y(n) = n \cdot x(n)$ and<br>(ii) $y(n) = x(n) - x(n-1)$ are time variant or time invariant.   | [2] | CO-1 | BL-1 |
| Q.1(b) Determine the output $y(n)$ of a relaxed linear time-invariant system with impulse response $h(n) = a^n u(n)$ , $a < 1$ , when the input is a unit step sequence, i.e. $x(n) = u(n)$ .                     | [3] | CO-1 | BL-3 |
| Q.2(a) Test the stability of LTI systems, whose impulse responses are<br>(i) $h(n) = 0.2^n u(n)$<br>(ii) $h(n) = 0.2^n u(-n) + 3^n u(-n)$   | [2] | CO-1 | BL-2 |
| Q.2(b) Obtain the direct form-II structure for the following system:<br>$y(n) = 3b^4 \cos \omega_0 y(n-1) - 2b^9 y(n-2) + 2x(n) - 6b \cos \omega_0 x(n-1)$ .  | [3] | CO-1 | BL-3 |
| Q.3(a) Determine $H(Z)$ , and its poles and zeros if<br>$y(n) + \frac{3}{4}y(n-1) + \frac{1}{8}y(n-2) = x(n) + x(n-1)$  | [2] | CO-2 | BL-3 |
| Q.3(b) A casual system is represented by the following difference equation.<br>$y(n) + \frac{1}{4}y(n-1) = x(n) + \frac{1}{2}x(n-1)$ . Find the system transfer function $H(z)$ , the impulse response of system. | [3] | CO-2 | BL-3 |
| Q.4(a) Determine the Z-Transform of the signal $h(n) = n \cdot a^n u(n)$ , $-1 < a < 1$   | [2] | CO-2 | BL-2 |
| Q.4(b) Using long division method, determine the inverse Z-transform of<br>$X(z) = \frac{1}{1 + \frac{5}{2}z^{-1} + 2z^{-2}}$ , when $ROC:  z  > 1$ .   | [3] | CO-2 | BL-3 |
| Q.5(a) Given a sequence $x(n) = \{1, 1, 0, 0\}$ , determine the discrete Fourier transform $X(K)$ .   | [2] | CO-3 | BL-2 |
| Q.5(b) Determine the IDFT of<br>$X(K) = \{3, 2+j, 1, 2 \cdot j\}$ .   | [3] | CO-3 | BL-3 |

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