

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: BTECH
BRANCH: ECE

SEMESTER : VI
SESSION : SP/2025

SUBJECT: EC359 INFORMATION THEORY AND CODING

TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Before attempting the question paper, be sure that you have got the correct question paper.
5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

		CO	BL
Q.1(a) Define basic concept of variable length coding. Is Huffman code a variable length code? Construct a Huffman code for a DMS with four symbols of equal probabilities and determine the maximum possible code efficiency for the code.	[5]	01	02
Q.1(b) Explain Arithmetic coding with an example. Also, consider a DMS with source probabilities {0.25, 0.25, 0.2, 0.15, 0.15} and design Shannon-Fano-Elias code. Also determine its average code word length.	[5]	01	04
Q.2(a) Prove that the information capacity of a continuous channel of bandwidth W hertz, perturbed by additive Gaussian noise of power spectral density $N_0/2$ is given by $C = W \log_2 \left(1 + \frac{P}{N_0 W} \right) \text{ bits/sec.}$	[5]	02	02
Q.2(b) Determine and compare the overall channel capacity of two cascaded connected binary symmetric channels if both have the same transition probability by taking three cases of transition probability: $p=0.3(<0.5)$, $p=0.5$ and $p=0.7(>0.5)$.	[5]	02	03
Q.3(a) Define Galois field and its properties. Prepare addition and multiplication table for the GF (3).	[5]	03	01
Q.3(b) Define Singleton and Humming bounds for linear block codes. Consider a parity check matrix $H = [1\ 0\ 0\ 0\ 0\ 1\ 1; 0\ 1\ 0\ 0\ 1\ 0\ 1; 0\ 0\ 1\ 0\ 1\ 1\ 0; 0\ 0\ 0\ 1\ 1\ 1\ 1]$, received sequence as $r = [0\ 0\ 1\ 1\ 0\ 1\ 1]$ and error $e = [0\ 1\ 0\ 1\ 0\ 0\ 0]$, then compute the syndrome, s and reconstructed code, c.	[5]	03	04
Q.4(a) For non-systematic coding in (7, 3) binary cyclic code (under GF (2)) with generator polynomial $g(x) = (1+x)(x^3+x+1)$. determine generator matrix, G & parity check matrix, H.	[5]	04	06
Q.4(b) Determine code polynomial/codeword for message $m(x) = 1 + x^2$. Assume systematic coding in (7, 3) binary cyclic code (under GF (2)). Take $g(x) = (1+x)(x^3+x+1)$	[5]	04	03
Q.5(a) Draw convolutional encoder, state diagram for the transfer function matrix $G(x) = [1(1+x+x^2)/(1+x^2)]$. Also determine the code rate and all possible output of this encoder.	[5]	05	04
Q.5(b) Determine the original message bits sent from the convolutional encoder with the transfer function matrix $G(x) = [x^2 + 1 \quad x^2 + x + 1]$ if the received sequence bits at Viterbi decoder of the convolutional code is $r = [11\ 10\ 11\ 01\ 11\ 01\ 00\ 01\ \dots]$	[5]	05	02

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