## BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (END SEMESTER EXAMINATION)

CLASS: BTECH SEMESTER: IV
BRANCH: CS/AIML SESSION: SP/2024

SUBJECT: CS241 DESIGN AND ANALYSIS OF ALGORITHM

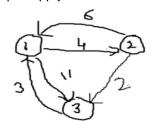
TIME: 3 Hours FULL MARKS: 50

## **INSTRUCTIONS:**

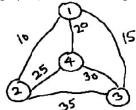
- 1. The question paper contains 5 questions each of 10 marks and total 50 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Before attempting the question paper, be sure that you have got the correct question paper.
- 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

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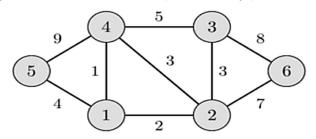
CO BL Q.1(a) Write an algorithm for insertion sort and find its complexity in best, average and worst [5] C01 Use a recursion tree to determine a good asymptotic upper bound on the [5] Q.1(b) CO1 4 recurrence  $T(n)=T(n/2)+n^2$ . Use the substitution method to verify it. Write the algorithm to sort the following list in descending order using Quick sort [5] 5 Q.2(a) CO2 technique and find its running time. L=(1, 3, 5, 6, 8, 10, 13, 18). Q.2(b) Write an algorithm to find the minimum and maximum element in the array using [5] CO2 3 divide and conquer. Find the its time complexity and trace the algorithm for the given array a=[ 22, 13, -5, -8, 15, 60, 17, 31, 47]. (Note that if the divide and conquer approach is not used, two marks will be deducted). Q.3(a) Write an algorithm to find the all pair shortest path using dynamic programming [5] CO3 2 technique. Apply the same for the given graph.



Q.3(b) Apply dynamic programming technique to solve the TSP Problem for the given [5] CO3 4 graph.(Assume starting vertex is 1).



Q.4(a) Write the kruskal's algorithm to find the MST, and trace the algorithm for the following [5] CO4 4 graph to find the MST with cost. (Show the steps)



Character	Frequency
Α	5
В	9
С	12
D	13
E	16
F	45

If the compression technique used is Huffman Coding, how many bits will be saved in the message? Draw the Huffman Tree. (Note that each character in input message takes 1 byte.)

Q.5(a) Define the classes P, NP hard and NP -complete. What do you mean by decision and [5] CO5 3 optimization problems?

Q.5(b) How satisfiability problem can be used to prove any other problem is an NP - Hard class? [5] CO5 4 Explain with suitable example.

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