## BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (END SEMESTER EXAMINATION)

CLASS: M.TECH. SEMESTER: II
BRANCH: CIVIL SESSION: SP/2024

## SUBJECT: CE506 FINITE ELEMENT METHOD

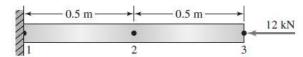
TIME: 3 HOURS FULL MARKS: 50

## **INSTRUCTIONS:**

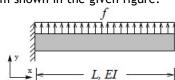
- 1. The question paper contains 5 questions each of 10 marks and total 50 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Before attempting the question paper, be sure that you have got the correct question paper.
- 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

- CO BL
- Q.1(a) Derive the global stiffness matrix for an axially loaded bar, inclined to x axis by an angle [5] 1 2  $\theta$ , of a plane truss using the element transformation.
- Q.1(b) A steel rod subjected to compression is modeled by two bar elements, as shown in the [5] 1 given figure. Determine the nodal displacements and the axial stress in each element.

  Take E = 200 GPa and A = 500 mm<sup>2</sup>.

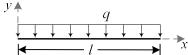


Q.2(a) Derive the method of weighted residual statements (both strong form and weak form) [5] 1 2 the beam shown in the given figure.



Q.2(b) Calculate the equivalent nodal load vector for the beam given in Figure 3. Interpolation [5] 1 4 functions for two-nodded beam element is given by

$$N_{1} = 1 - \frac{3x^{2}}{L^{2}} + \frac{2x^{3}}{L^{3}}, \quad N_{2} = x - \frac{2x^{2}}{L} + \frac{x^{3}}{L^{2}}, \quad N_{3} = \frac{3x^{2}}{L^{2}} - \frac{2x^{3}}{L^{3}}, \quad N_{4} = -\frac{x^{2}}{L} + \frac{x^{3}}{L^{2}}$$

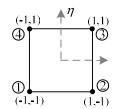


Q.3(a) Use Galerkin's method of weighted residuals to obtain an approximate solution of the [5] 1 differential equation.

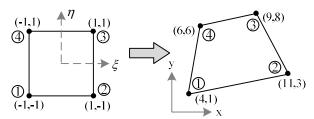
$$\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} - 5x^2 = 3 \qquad 0 \le x \le 1$$

With boundary condition y(0) = 0, y(1) = 0.

Q.3(b) Derive the polynomial form of all the shape functions (  $N_{\rm l}$  -  $N_{\rm d}$  ) for the following rectangular element. [5] 3 3



Q.4(a) Derive the Jacobian matrix for the isoperimetric mapping of linear element (shown in [5] 3 the figure). Use the shape function derived in Q.3(b).



Q.4(b) Evaluate the following integral using 2-point Gauss quadrature:

- $\int_{-1}^{1} \int_{-1}^{1} (1 + 2x + 3x^{2}y) \, dx \, dy$
- Q.5(a) Explain the following steps in context of any commercial FE Application:
- [5] 2 1

- a) Pre-Processing
- b) Analysis
- c) Post-processing
- Q.5(b) Derive then relation between the derivates with respected global Cartesian co-ordinates [5] 3 2 (x, y) and local co-ordinates ( $\xi$ ,  $\eta$ ) for isoperimetric mapping of 2D rectangular element.

:::::23/04/2024 E:::::