

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(MID SEMESTER EXAMINATION SP2023)

CLASS: BTECH  
BRANCH: MECHANICAL

SEMESTER : VI  
SESSION : SP2023

SUBJECT: ME353 COMPUTATIONAL FLUID DYNAMICS

TIME: 02 Hours

FULL MARKS: 25

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

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		CO	BL
Q.1(a)	What are the basic physical principles associated with fluid flow and heat transfer, and what are the associated equations commonly known as?	[2] 1	1
Q.1(b)	State and prove the physical significance of the divergence of velocity vector in a flow field.	[3] 1	2
Q.2(a)	Derive the continuity equation for fluid flow in the conservation form for an infinitesimally small control volume.	[3] 1	3
Q.2(b)	Show the equivalence of the above equation to the conservation for a finite control volume.	[2] 1	3
Q.3(a)	Classify quasilinear Partial Differential Equations (PDEs) of 2 <sup>nd</sup> order, stating their mathematical conditions for a simple linear 2-D equation of 2 <sup>nd</sup> order.	[2] 2	1
Q.3(b)	Giving simple examples of physical equations of heat transfer, fluid flow, etc, illustrate the different categories of PDEs mentioned above, and briefly state the physical characteristics associated with them.	[3] 2	2
Q.4(a)	Prove the following relation for the first order derivative of a variable $\phi$ with respect to the x-dimension, where all the symbols carry usual meaning as discussed in the class. What is the order of accuracy?	[5] 3	4
	$\frac{\partial \phi}{\partial x} = \frac{1}{2h} \left[ \frac{\overline{\delta_x \phi}}{1 + \frac{\delta_x}{6}} \right]$		
Q.5(a)	Define consistency of a numerical scheme. Show that central difference scheme applied to discretize the Laplace equation is consistent. What is the associated order of the truncation error?	[2] 3	2
Q.5(b)	What are the 4 types of iterative methods to solve any discretized algebraic equation over a space domain. Briefly discuss the application of Tri-Diagonal-Matrix Algorithm (TDMA), showing the sequential steps involved.	[3] 3	3

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