

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- Q.1(a) A vector  ${}^A P$  is rotated about  $\hat{Z}_A$  by an angle  $\theta$  and is subsequently rotated about  $\hat{X}_A$  by an angle  $\phi$ . Evaluate the rotational matrix that accomplishes these rotations in the given order. [2] 1 Evaluate
- Q.1(b) Two frames {A} and {B} are related by the following matrix: [3] 1 Sketch
- $${}^A T_B = \begin{bmatrix} 0 & 1 & 0 & 15 \\ -1 & 0 & 0 & 20 \\ 0 & 0 & 1 & -9 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
- If the orientation vector of a parameter is given in frame {B} as  ${}^B V = \begin{pmatrix} 10 \\ 10 \\ 10 \end{pmatrix}$ , what is its orientation in {A}? Also, sketch frame {B} relative to frame {A}.
- Q.2 {A} and {B} are frames differing only in orientation. {B} is attained as follows: [5] 1 Evaluate  
starting coinciding with {A}, {B} is rotated by  $\theta$  radians about unit vector  $\hat{K}$ , i.e.,  ${}^A R_B = {}^A R_K(\theta)$ . Show that  ${}^A R_B = e^{K\theta}$ , where
- $$K = \begin{bmatrix} 0 & -k_z & k_y \\ k_z & 0 & -k_x \\ -k_y & k_x & 0 \end{bmatrix}$$
- Q.3(a) Write the name of the point where the tool frame should be affixed. [1] 1 Write
- Q.3(b) Show the attachment of the link frames and derive the DH-parameter of the manipulator shown in Fig. Q.3(b). [4] 1 Derive

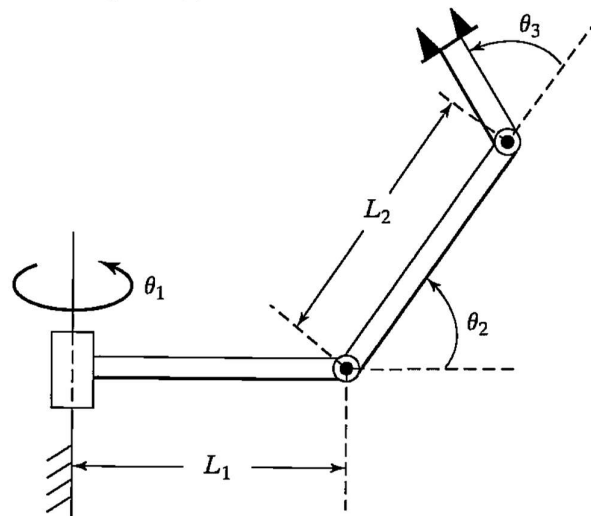


Fig. Q.3(b)

Q.4(a) Define repeatability and accuracy.

[2] 2 Define

Q.4(b) Derive inverse-kinematics solution for  $d_2$  and  $d_3$  shown in Fig. Q.4(b).

[2] 2 Derive

[3]

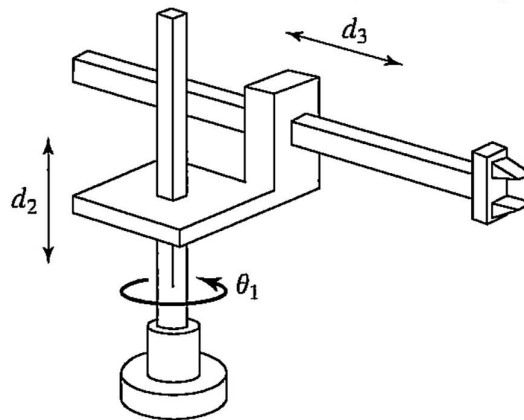


Fig. Q.4(b)

Q.5(a) For a manipulator derive Jacobian in force domain.

[2] 2 Derive

Q.5(b) The two-link manipulator (shown in Fig. Q.5(b)) is applying a force vector  ${}^3F$  with its end-effector. Consider this force to be acting at the origin of  $\{3\}$ . Find the required joint torques as a function of configuration and of the applied force.

[3] 2 Find

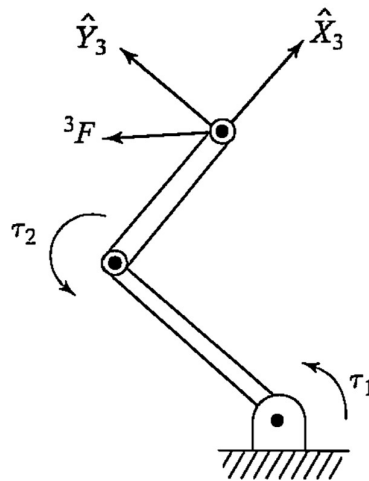


Fig. Q.5(b)

Hint:

$$R_K(\theta) = \begin{bmatrix} k_x k_x v\theta + c\theta & k_x k_y v\theta - k_z s\theta & k_x k_z v\theta + k_y s\theta \\ k_x k_y v\theta + k_z s\theta & k_y k_y v\theta + c\theta & k_y k_z v\theta - k_x s\theta \\ k_x k_z v\theta - k_y s\theta & k_y k_z v\theta + k_x s\theta & k_z k_z v\theta + c\theta \end{bmatrix}$$

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