

# BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI End Semester: MTECH - II (SP/2022) ME510: Advanced Vibration & Simulation

Total Marks = 50 Time: 2 Hours

## INSTRUCTIONS

- Attempt all the questions.
- The missing data, if any, may be assumed suitably.
- Students should write their full name, Roll No., course code and course name on the answer sheet.

### MODULE 1

 Q1.1 Derive the governing equation of motion for a simple spring-mass system corresponding to Figure 1.1.
 [5 marks]

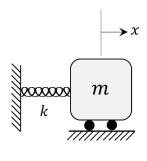
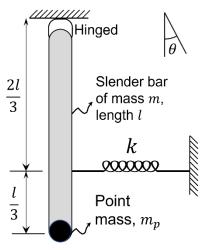


Figure 1.1



### Figure 1.2

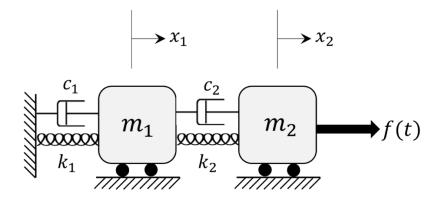
**Q1.2** Determine the governing equation of motion for small oscillations about the vertical equilibrium position for Figure 1.2. Use  $\theta$  as the chosen generalized coordinate.

[5 marks]

Q1.3 Name atleast 4 damping models used in vibration analysis. [4 marks]

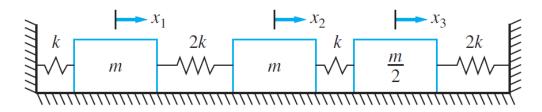
### MODULE 2

- Q2.1 For a beam of total length l, write down the boundary conditions at its both ends namely x = 0 and x = l for the following cases. [1+1+1+2 marks]
  - Both ends free
  - Both ends fixed
  - One end fixed and another end is free
  - Simply supported ends
- Q2.2 For the system shown below, draw the free body diagram and derive the governing equations of motion, clearly mentioning the Law used. [5 marks]



#### MODULE 3

Q3.1. Using Matrix iteration method find the first three natural frequencies of the following system. [5 marks]



Q3.2. Determine the fundamental frequency of the vibration of the system using Dunkerley's method for the <u>above</u> system. [5 marks]

#### MODULE 4

- **Q4.1** Consider free Duffing equation as  $\ddot{x} + \omega_n^2 x + \beta x^3 = 0$ ; where  $\beta$  is very small to incorporate weak non-linearity. Find the solution of the equation comprising of both complimentary function and particular integral. [5 marks]
- Q4.2 Explain the Jump phenomenon with a neat diagram. [3 marks]
- Q4.3 Write the Mathieu equation explaining the parameters involved and give one example of it's applicability. [4 marks]

#### MODULE 5

Q5.1. Explain the basic principle of operation of electrodynamic shaker with a neat diagram. [4 marks]

29/04/2022