

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(END SEMESTER EXAMINATION)**

**CLASS: BE  
BRANCH: EEE**

**SEMESTER : IV/ADD  
SESSION : SP/19**

**SUBJECT EE4207-DIGITAL SIGNAL PROCESSING**

**TIME: 3 Hours**

**FULL MARKS: 60**

**INSTRUCTIONS:**

1. The question paper contains 7 questions each of 12 marks and total 84 marks.
  2. Candidates may attempt any 5 questions maximum of 60 marks.
  3. The missing data, if any, may be assumed suitably.
  4. Before attempting the question paper, be sure that you have got the correct question paper.
  5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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- Q.1(a) Find the relationship between Discrete-Fourier Transform to Discrete-Time Fourier Series [2]  
Q.1(b) Distinguish between linear convolution and circular convolution. [4]  
Q.1(c) Given  $x(n) = \{0,1,2,3,4,5,6,7\}$ , find 8-point DFT  $X(k)$  using the DIT-FFT algorithm. Show all the intermediate results. [6]
- Q.2(a) The following specifications are given for an LPF:  $\Omega_p = 1$ ,  $\Omega_s = 2.33$ ,  $A_p = 0.5$  dB,  $A_s = 22$  dB. Compute the filter order for a Chebyshev and a Butterworth analog filter. [2]  
Q.2(b) Write the comparison characteristics between IIR and FIR filter. [4]  
Q.2(c) Design an IIR low-pass Butterworth filter using the impulse invariant method for the following specifications Pass band:  $0.8 \leq |H(e^{j\omega})| \leq 1$   $|\omega| \leq 0.2\pi$   
Stop band:  $|H(e^{j\omega})| \leq 0.2$   $0.6\pi \leq |\omega| \leq \pi$ . Assume  $T = 1$  sec. [6]
- Q.3(a) Explain the scaling and differentiation property of Z-transform? [2]  
Q.3(b) What is the Gibbs phenomena? [4]  
Q.3(c) Explain the given system  $\sum_{k=-\infty}^n x(k)$  with respect to following properties (i) Dynamicity (ii) Time invariance (iii) Linearity (iv) Causality (v) Stability [6]
- Q.4(a) Write the comparisons for the window, frequency sampling and optimal methods for linear- phase finite impulse response filters. [2]  
Q.4(b) Determine the frequency response (DTFT) of causal rectangular window of length  $N$ ? [4]  
Q.4(c) Design an FIR filter to meet the following specifications: ( i ) pass band edge :  $F_p = 2$  KHz, (ii) stop band edge:  $F_s = 5$ KHz (iii) pass band attenuation:  $A_p = 2$  dB (iv) stop band attenuation:  $A_s = 42$  dB (v) sampling frequency :  $F_T = 20$  KHz [ Don't evaluate frequency response] [6]
- Q.5(a) List the three properties of DFT. [2]  
Q.5(b) Determine the impulse response for the cascaded of two linear time-invariant systems having impulse responses  $h_1(n) = (1/2)^n u(n)$  and  $h_2(n) = (1/4)^n u(n)$ . [4]  
Q.5(c) Determine the inverse Z-transform of the  $X(z) = (z+2) / (2z^2-7z+3)$  if the ROCs are (i)  $|z| > 3$  (ii)  $|z| < (1/2)$  (iii)  $(1/2) < |z| < 3$ . [6]
- Q.6(a) Distinguish between the following: (i) Energy and Power signal (ii) Multichannel and Multidimensional. [2]  
Q.6(b) Consider the analog signal  $X_a(t) = 3\cos(2000\pi t) + 5\sin(6000\pi t) + 10\cos(12000\pi t)$   
(i) what is the Nyquist rate for this signal? (ii) if we sampled this signal with the sampling rate 5000 samples/s. What is the discrete time signal after sampling? [4]  
Q.6(c) The accumulator described by  $\sum_{k=-\infty}^n x(k) = y(n)$  is excited by the sequence  $x(n) = nu(n)$ . Determine its output under the condition (i) It is initially relaxed (ii) Initially,  $y(-1) = 1$  [6]
- Q.7(a) Estimate the filter order of a linear-phase low-pass FIR filter using Kaiser formula with the following specifications: Pass band edge frequency = 1.8 KHz, Stop-band edge frequency = 3 KHz, Maximum pass-band attenuation = 6.1 dB, Minimum stop-band attenuation = 35 dB, and sampling frequency= 12 KHz. [2]  
Q.7(b) Describe the relationship between analog and digital, filter poles and frequencies in Impulse- Invariant Transformation. [4]  
Q.7(c) Obtain the direct-form II structure of the system described by difference equation. [6]  
 $y(n) = 2r \cos(\omega_0) y(n-1) - r^2 y(n-2) + x(n) - r \cos(\omega_0) x(n-1)$