

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: IMSc
BRANCH: Physics

SEMESTER : III
SESSION : MO/2025

SUBJECT: PH24205 MATHEMATICAL PHYSICS I

TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Before attempting the question paper, be sure that you have got the correct question paper.
 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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|-----|---|------|-------|---------|
| Q.1 | Find the eigenvalues and normalised eigenfunctions of the matrix $\begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta & -\sin\theta \\ 0 & \sin\theta & \cos\theta \end{pmatrix}$. | [10] | 1 | 1,2 |
| Q.2 | If $\vec{F} = 2y\hat{i} - z\hat{j} + x\hat{k}$. Evaluate $\int_C \vec{F} \times \overline{dr}$ along the curve $x = \cos t, y = \sin t, z = 2\cos t$, from $t = 0$ to $t = \pi/2$. | [10] | 2 | 2,3 |
| Q.3 | Find a complex Fourier series expansion of $f(x) = x, -2 < x < 2$. | [10] | (a) 3 | (l) 2,3 |
| Q.4 | Define convolution between two functions and prove the convolution theorem. | [10] | 4 | 2,3 |
| Q.5 | Find the inverse Laplace transform of $\frac{8}{s^3(s+2)}$. | [10] | 5 | 2,3 |

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