

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION)

CLASS: BTECH
BRANCH: MECH

SEMESTER : V/ADD
SESSION : MO/2025

SUBJECT: ME355 ADVANCED SOLID MECHANICS

TIME: 02 Hours

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates
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- Q.1 The state of stress at a point is such that CO BL
[5] 1 4

$$[\sigma_{ij}] = \begin{bmatrix} 0 & -75 & -55 \\ -75 & 0 & 65 \\ -55 & 65 & 0 \end{bmatrix} MPa$$

Determine the principal stresses and their directions.

- Q.2 Explain what is meant by octahedral stresses and their significance in stress analysis. [5] 1 2
Derive the expressions for octahedral normal stress and octahedral shear stress in terms of principal stresses.

- Q.3 Consider the displacement field: $u = [y^2i + 3yzj + (4 + 6x^2)k]10^{-2}$. What are the rectangular strain components at point P (1, 0, 2)? Use only linear terms. [5] 1 4

- Q.4 Explain the behavior of a beam-column subjected to axial and lateral loads. Discuss why the principle of superposition does not directly apply in this case and write down the governing differential equation for beam-column deflection. [5] 2 2

- Q.5 A simply supported pin-ended column of length L , modulus of elasticity E and moment of inertia I is subjected to an axial compressive load P . Assume the buckled shape of the column is given by [5] 2 3

$$y(x) = a \sin(\pi x/L)$$

Where a is an unknown parameter. Using the Rayleigh-Ritz method and the minimum total energy principle:

- i. Find expressions for the elastic strain energy U_b due to buckling of the column and potential energy U_p due to the applied compressive load P using $y(x)$.
- ii. Find the expression for the total potential energy $U_b + U_p$.
- iii. Determine the critical load P_{cr} for buckling.

:::22/09/2025 :::M