

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION)

CLASS: BTECH
BRANCH: CSE/AI ML

SEMESTER : III
SESSION : MO/2025

SUBJECT: MA24205 DISCRETE MATHEMATICS

TIME: 02 Hours

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates
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|--------|---|---------|----|
| Q.1(a) | Identify which of the following propositions are statements? | [2] CO1 | 2 |
| | i. Rome is the capital of Spain | | |
| | ii. $x + 2 = 11$ | | |
| Q.1(b) | Determine whether the given statement is a tautology, a contingency, or a contradiction. | [3] CO1 | 4 |
| | i. $q \vee (\sim q \wedge p)$ | | |
| | ii. $(p \wedge q) \Rightarrow p$ | | |
| Q.2(a) | Find a truth table for $(p \vee q) \Rightarrow (p \wedge q)$ | [2] CO1 | 1 |
| Q.2(b) | Let a and b be real numbers. Using mathematical induction prove that $(a \cdot b)^n = a^n \cdot b^n$ for all natural numbers n . | [3] CO1 | 3 |
| Q.3 | Find a particular solution of the recurrence relation $a_{r+1} - a_r = r^2$ | [5] CO2 | 1 |
| Q.4 | Solve the recurrence relation $a_{n+2} - 5a_{n+1} + 6a_n = 2$ by the method of generating function with initial conditions $a_0 = 1, a_1 = 3$. | [5] CO2 | 3 |
| Q.5(a) | Define cartesian product of two sets A and B . If a set has 100 elements, what is the cardinality of its power set ? | [2] CO3 | 1 |
| Q.5(b) | Let A be the set of positive integers, and let R be the relation $R = \{(a, b) \in A \times A \mid a \text{ divides } b\}$. Determine whether R symmetric, asymmetric, or antisymmetric? | [3] CO3 | 4 |

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