

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: BTECH

BRANCH: Mech/Prod/Civil/Biotech/Chemical/Food Tech

SUBJECT: MA24201 NUMERICAL METHODS

SEMESTER : III/ADD

SESSION : MO/2025

TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Before attempting the question paper, be sure that you have got the correct question paper.
5. Tables/Data handbook/Graph paper etc. to be supplied to the candidates in the examination hall.

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| | | O | L | | | | | | | | | | | | |
| Q.1(a) if $u = 4x^2y^3/z^4$ and error in x, y, z are 0.001, compute the relative maximum error in u when $x = y = z = 1$. [5] | 1 | 2 | | | | | | | | | | | | | |
| Q.1(b) Find the root of the equation $\cos x = xe^x$ in the interval (0.50995, 1) using the regula-falsi method correct to four decimal places. [5] | 1 | | 3 | | | | | | | | | | | | |
| Q.2(a) Use LU Decomposition method to solve the following equation:
$3x + 2y + 7z = 4; 2x + 3y + z = 5; 3x + 4y + z = 7$. [5] | 2 | | 2 | | | | | | | | | | | | |
| Q.2(b) Solve by Jacobi's iteration method, the equations
$10x + y - z = 11.19, x + 10y + z = 28.08, -x + y + 10z = 35.61$, correct to two decimal places. [5] | 2 | | 3 | | | | | | | | | | | | |
| Q.3(a) A curve passes through the points (0,18), (1,10), (3,-18) and (6,90). Find the slope of the curve at $x=2$. [5] | 3 | | 2 | | | | | | | | | | | | |
| Q.3(b) Find the missing term in the following table using interpolation: [5] | 3 | | 3 | | | | | | | | | | | | |
| <table border="1" style="margin: auto; border-collapse: collapse;"> <tr> <td style="padding: 2px;">x:</td> <td style="padding: 2px;">0</td> <td style="padding: 2px;">1</td> <td style="padding: 2px;">2</td> <td style="padding: 2px;">3</td> <td style="padding: 2px;">4</td> </tr> <tr> <td style="padding: 2px;">y:</td> <td style="padding: 2px;">1</td> <td style="padding: 2px;">3</td> <td style="padding: 2px;">9</td> <td style="padding: 2px;">...</td> <td style="padding: 2px;">81</td> </tr> </table> | | | | x: | 0 | 1 | 2 | 3 | 4 | y: | 1 | 3 | 9 | ... | 81 |
| x: | 0 | 1 | 2 | 3 | 4 | | | | | | | | | | |
| y: | 1 | 3 | 9 | ... | 81 | | | | | | | | | | |
| Q.4(a) Evaluate the integral $\int_0^1 \frac{x^2}{1+x^2} dx$ using Simpson's 1/3 rule. Compare the error with the exact value. Take four equal parts of the interval. [5] | 4 | | 2 | | | | | | | | | | | | |
| Q.4(b) Compute the value of the integral $\int_{0.2}^{1.4} (\sin x - \log x + e^x) dx$ using Simpson's 3/8 rule by taking seven ordinates. [5] | 4 | | 3 | | | | | | | | | | | | |
| Q.5(a) Using modified Euler's method, find an approximate value of y when $x=0.2$ and 0.4 , given
$\frac{dy}{dx} = y + e^x$ and $y = 0$ when $x = 0$. Take $h=0.2$. [5] | 5 | | 2 | | | | | | | | | | | | |
| Q.5(b) Using the Runge-Kutta method of fourth order, solve for y at $x=1.2$ and 1.4 from
$\frac{dy}{dx} = \frac{2xy + e^x}{xe^x + x^2}$ given $y(1) = 0$. [5] | 5 | | 3 | | | | | | | | | | | | |