

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(END SEMESTER EXAMINATION)**

CLASS: BTECH  
BRANCH: EEE

SEMESTER : VII  
SESSION : MO/2025

SUBJECT: EE439 APPLIED CONTROL THEORY

TIME: 3 Hours

FULL MARKS: 50

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Before attempting the question paper, be sure that you have got the correct question paper.
5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

Q.1(a) The state variable description is  $\dot{x} = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u$  [5] CO BL

Determine state transition matrix of the system assuming all initial condition is zero

Q.1(b)  $\dot{x} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$  [5]

$Y = [1 \ 0] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$  Find the Unforce response of the system.

Q.2(a) A system is represented by [5]

$$\dot{x} = \begin{bmatrix} -1 & 3 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u$$

$$y = [1 \ 0] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

Designee a state feedback controller for the given system such that the close loop pole are at -5 and -6.

Q.2(b) For the system given below, an observer is to be designed to estimate the state variables. [5]  
Select the observer gain and write the equations describing the observer dynamics.

$$\dot{x} = \begin{bmatrix} -4 & -4 \\ 1 & -2 \end{bmatrix} x + \begin{bmatrix} 0 \\ 2 \end{bmatrix} u$$

$$y = [1 \ 0] x$$

Observer eigen value should be (-10,-10).

Q.3(a) Consider a nonlinear system defined as [5]

$$\dot{x}_1 = x_2$$

$$\dot{x}_2 = -\frac{n}{m} x_2^2 + \frac{1}{m} u$$

Where m and n are constant. Linearize the state equation.

Q.3(b) Define describing Function and explain its significance in the analysis of nonlinear system. [5]  
Derive the describing function of an Idel Relay.

Q.4(a) Consider the system describe as [5]

$$\ddot{y} + \dot{y} + y - y^2$$
 Draw the Phase trajectory of the system.

Q.4(b) Draw the shape of the phase portrait for the following singular point [5]  
1) Node, 2) Focus, 3) Center, 4) Saddle.

Q.5(a) Explain the different type of optimal control problem. [5]

Q.5(b) Find the extremal curve for the functional  $J(x) = \int_0^1 \frac{1}{\dot{x}} dt$  [5]

The boundary condition are given  $x(0)=0, x(1)= 1$