

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION)

CLASS: IMSc
BRANCH: QEDS

SEMESTER : V/ADD
SESSION : MO/2025

SUBJECT: ED307 PARAMETRIC INFERENCE

TIME: 02 Hours

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates
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- Q.1 Let X_1, X_2, \dots, X_5 be a sample of size 5 from the uniform distribution on the interval $(0, \theta)$, where θ is unknown. Let the estimator of θ be $k X_{max}$, where k is some constant and X_{max} is the largest observation. In order $k X_{max}$ to be an unbiased estimator, what should be the value of constant k ? [5] CO C01 BL III
- Q.2 Show that $\bar{X} = \sum_{i=1}^n X_i/n$, in random sampling from $f(x, \theta) = \begin{cases} \frac{1}{\theta} \exp(-x/\theta) & x > 0 \\ 0 & \text{otherwise} \end{cases}$ where $0 < \theta < \infty$ is an uniformly minimum variance unbiased estimator for θ . [5] C01 II
- Q.3 If X_1, X_2, \dots, X_n is a random sample from the density function: $f(x, \theta) = \begin{cases} 1 & \theta < x < \theta + 1 \\ 0 & \text{otherwise} \end{cases}$ Show that the sample mean \bar{X} is an unbiased and consistent estimator for $\theta + \frac{1}{2}$. [5] C01 II
- Q.4 Let X_1, X_2, \dots, X_n be a random sample from a distribution with probability density function : $f(x, \theta) = \begin{cases} 3 \theta x^2 e^{-\theta x^2} & \text{for } 0 < x < \infty \\ 0 & \text{otherwise,} \end{cases}$ where $\theta > 0$ is an unknown parameter. Find a sufficient statistic for θ . [5] C02 III
- Q.5 If $f(x; \theta_1, \theta_2) = \frac{1}{B(\theta_1, \theta_2)} x^{\theta_1-1} (1-x)^{\theta_2-1}$, then check whether it belongs to the exponential family and find the joint sufficient statistics for θ_1 and θ_2 . [5] C02 V

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