

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION)**

CLASS: IMSC
BRANCH: QEDS

SEMESTER : III
SESSION : MO/2025

SUBJECT: ED24211 LINEAR MODELS AND REGRESSION ANALYSIS

TIME: 02 HOURS

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- | | | | | |
|--|-----|---|----|----|
| Q.1(a) Define the simple linear regression model with all possible assumptions. | [2] | 1 | CO | BL |
| Q.1(b) Estimate the parameters in simple linear regression using normal equation | [3] | 1 | | |

- | | | | | |
|---|-----|---|--|--|
| Q.2(a) Define design matrix, response vector, predicted response vector, sum of squared error, sum of squared total for a simple linear regression with given data set $\{(x_i, y_i)\}_{i=1}^n$ | [2] | 1 | | |
| Q.2(b) Predicting exam score based on hours studied from the following data set: | [3] | 1 | | |

X (study hours)	2	4	6	8	10
Y (exam score)	50	55	65	70	80

- | | | | | |
|--|-----|---|--|--|
| Q.3(a) Define the multiple linear regression model with all possible assumptions. | [2] | 3 | | |
| Q.3(b) Estimate the parameters in multiple linear regression using normal equation | [3] | 3 | | |

- | | | | | |
|---|-----|---|--|--|
| Q.4(a) Predicting crop yield based on rainfall and fertilizer from the following dataset: | [2] | 3 | | |
|---|-----|---|--|--|

x1 (rainfall in mm)	100	120	130	150	170
x2 (fertilizer in kg)	50	60	65	70	80
Y (crop yield)	200	220	230	250	270

- | | | | | |
|--|-----|---|--|--|
| Q.4(b) Compute predicted response vector, sum of squared error, sum of squared total for a simple linear regression with the dataset of Q.4(a) | [3] | 3 | | |
|--|-----|---|--|--|

- | | | | | |
|--|-----|---|--|--|
| Q.5(a) Explain forward, backward and stepwise regressions for variable selections in a multiple regression | [2] | 3 | | |
|--|-----|---|--|--|

- | | | | | |
|--|-----|---|--|--|
| Q.5(b) Explain which one is the first incoming predictor in the following result of partial linear regression: | [3] | 3 | | |
|--|-----|---|--|--|

Predictor	Coef	SE Coef	T	P
Constant	81.479	4.927	16.54	0.000
x1	1.8687	0.5264	3.55	0.005

Predictor	Coef	SE Coef	T	P
Constant	57.424	8.491	6.76	0.000
x2	0.7891	0.1684	4.69	0.001

Predictor	Coef	SE Coef	T	P
Constant	110.203	7.948	13.87	0.000
x3	-1.2558	0.5984	-2.10	0.060

Predictor	Coef	SE Coef	T	P
Constant	117.568	5.262	22.34	0.000
x4	-0.7382	0.1546	-4.77	0.001