

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(END SEMESTER EXAMINATION)**

CLASS: B.Tech  
BRANCH: ECE

SEMESTER : 5<sup>th</sup> /ADD  
SESSION : MO/2025

SUBJECT: EC305: SIGNAL PROCESSING TECHNIQUES

TIME: 3 Hours

FULL MARKS: 50

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
  2. Attempt all questions.
  3. The missing data, if any, may be assumed suitably.
  4. Before attempting the question paper, be sure that you have got the correct question paper.
  5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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		CO	BL
Q.1(a) Distinguish between linear convolution, circular (periodic) convolution, and deconvolution in discrete-time signal processing. By means of circular convolution, determine the response of the FIR filter with impulse response $h(n) = \{4, 1, 3\}$ to the input sequence $x(n) = \{2, 5, 0, 4\}$	[5]	1	2,3
Q.1(b) What is the differentiation property of the z-transform? Use the differentiation property of the z-transform to find the z-transform of $g(n) = n a^n u(n)$	[5]	1	2,3
Q.2(a) Explain the conversion of direct form-I structure to direct form-II structure with an example. Compare the computational complexity in the direct form-I and direct form-II structures of IIR filters	[5]	2	2,3
Q.2(b) Obtain the direct form I and II realisation structures for the following system: $y(n) = -0.1y(n-1) + 0.72y(n-2) + 0.7x(n) - 0.25x(n-2)$	[5]	2	1,2,3
Q.3(a) Differentiate between the Butterworth and Chebyshev filters. Describe the frequency transformation in the analog & digital domain.	[5]	3	2,3
Q.3(b) A digital Butterworth filter has to be designed using bilinear transformation. The filter specifications are as follows: $0.9 \leq  H(e^{j\omega})  \leq 1 \quad 0 \leq \omega \leq 0.5\pi$ $ H(e^{j\omega})  < 0.2 \quad 0.75\pi < \omega < \pi$ Find the filter order N and the cut-off frequency $\Omega_c$	[5]	3	2,3,4
Q.4(a) Derive the relation between analog and digital frequency in impulse invariant transformation	[5]	4	1,2
Q.4(b) For the analog transfer function, $H(s) = \frac{2}{s^2 + 3s + 2}$ , determine H(z) using bilinear transformation if T = 1 second	[5]	4	2
Q.5(a) Describe multi rate signal processing. Explain Decimation and interpolation with suitable example.	[5]	5	1,2
Q.5(b) The transfer function of an FIR filter is $H(z) = 0.2 + 0.7z^{-1} + 0.8z^{-2} + 0.15z^{-3} + 0.6z^{-4} + 0.32z^{-5} + 0.5z^{-6} + 0.4z^{-7} + 0.9z^{-8}$ Perform polyphase decomposition of $H(z)$ to decompose into 2 sections	[5]	5	2,3