BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (END SEMESTER EXAMINATION)

CLASS: IMSc / MSc SEMESTER: VII/I
BRANCH: PHYSICS SESSION: MO/2024

SUBJECT: PH404 QUANTUM MECHANICS

TIME: 3 Hours FULL MARKS: 50

INSTRUCTIONS:

- 1. The question paper contains 5 questions each of 10 marks and total 50 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Before attempting the question paper, be sure that you have got the correct question paper.
- 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

| Q.1(a) | Prove that eigenvalues of an Hermitian matrix \boldsymbol{H} are real and eigenfuntions correspoding to different eigenvalues of \boldsymbol{H} are orthogonal. | [10] | CO 1 | BL 1,2 |
|--------|---|------|---------|-----------|
| Q.2(a) | Write down the postulates of quantum mechanics and provide an algorithm to find the propagator for any quantum system. | [10] | 2 | 1,2 |
| Q.3(a) | Find the average momentum of the electron in a Hydrogen atom in the ground state $\psi_{100} = \frac{1}{\sqrt{\pi a_0^3}} \exp\left(-r/a_0\right)$ given by | [10] | 3 | 2,3 |
| Q.4(a) | Find the eigenvalues and normalised eigenfunctions of S_x , S_y and S_z operators. | [10] | 4 | 1,2 |
| Q.5(a) | Find the matrix elements of $S_1 \cdot S_2$ in the product basis of two spin-half particles. | [10] | 5 | 2,3 |

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