

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: IMSc
BRANCH: Physics

SEMESTER : V
SESSION : MO/2024

SUBJECT: PH301 QUANTUM MECHANICS AND APPLICATIONS (QMA)

TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Before attempting the question paper, be sure that you have got the correct question paper.
5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

| | | CO | BL |
|--------|---|-------|----|
| Q.1(a) | Establish time dependent Schrodinger wave equation? | [5] 1 | 1 |
| Q.1(b) | Find the expectation value of position and momentum of a particle whose normalized wave function is | [5] 1 | 3 |
| | $\psi(x) = Ne^{-(x^2/2a^2)+ikx}$ | | |
| Q.2(a) | What is the significance of the momentum wave-function. Write down its forms in terms of propagation constant? | [5] 2 | 2 |
| Q.2(b) | For a Gaussian function f(x) represented by $f(x) = \frac{1}{\sqrt{(\sigma\sqrt{\pi})}} e^{-x^2/2\sigma^2}$ where σ determines the width of the wave-packet. Using Fourier transform derive the amplitude function A(k)? | [5] 2 | 3 |
| Q.3(a) | For a quantum particle undergoing harmonic oscillation, show that the energy Eigen values are expressed as $E_n = \left(n + \frac{1}{2}\right) \hbar\omega$ | [5] 3 | 2 |
| Q.3(b) | Calculate the energy difference between the ground state and first excited state for an electron in one dimensional rigid box of length 10^{-10} m? ($m_e = 9.1 \times 10^{-31}$ Kg, $h = 6.626 \times 10^{-34}$ joule-sec) | [5] 3 | 3 |
| Q.4(a) | For the radial part of Hydrogen atom given by $\frac{\partial^2 R}{\partial r^2} + \frac{2}{r} \frac{\partial R}{\partial r} + \left[\frac{-l(l+1)}{r^2} + \frac{2\mu}{\hbar^2} \{E - V(r)\} \right] R = 0$ Setup the recursion relation $a_{k+1} = \frac{k+l+1-\lambda}{(k+1)(2l+k+2)} a_k$ Given $\alpha^2 = -\frac{2\mu E}{\hbar^2}$ and $\lambda = \frac{\mu Z e^2}{\hbar^2 \alpha}$ and show energy eigen-values are given by $E_n = -\frac{\mu Z^2 e^4}{2\hbar^2 n^2}$ | [5] 4 | 2 |
| Q.4(b) | The wave function of Hydrogen atom for the 1s state is $\psi(1s) = \frac{1}{\sqrt{\pi}} \left(\frac{1}{a_0} \right)^{3/2} e^{-r/a_0}, \text{ Where, } a_0 = \frac{\hbar^2}{me^2} \text{ is the Bohr's radius. Calculate the expectation value of the potential energy of electron in 1s state.}$ | [5] 4 | 3 |
| Q.5(a) | Derive the expression for the Larmor's Precession frequency? | [5] 5 | 2 |
| Q.5(b) | Discuss the Stern-Gerlach experiment and its significance? | [5] 5 | 1 |