## BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (MID SEMESTER EXAMINATION MO/2024)

SEMESTER: III

CLASS:

**IMSc** 

**BRANCH: PHYSICS** SESSION: MO/2024 SUBJECT: PH105R2 MATHEMATICAL PHYSICS I TIME: 02 Hours **FULL MARKS: 25 INSTRUCTIONS:** 1. The question paper contains 5 questions each of 5 marks and total 25 marks. 2. Attempt all questions. 3. The missing data, if any, may be assumed suitably. 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates \_\_\_\_\_ CO BL Q.1 Show that the eigenvalues, trace and determinant of a matrix are unchanged [5] 1 1,2 under a change of basis or a similarity transformation. Find the eigenvalues and normalised eigenfunctions of the matrix  $\begin{pmatrix} cos\theta & sin\theta \\ -sin\theta & cos\theta \end{pmatrix}$ . Q.2 [5] 2,3 Q.3 State the Gauss theorem, Stokes theorem and Green's theorem. 2 [5] 1,2 Q.4 Give physical interpretation of gradient, divergence and curl. 2,3 2 [5] Evaluate  $\int_{(1,0)}^{(-1,0)} \frac{-ydx+xdy}{x^2+y^2}$  along the following paths: Q.5 [5] 2 2,3 (a) Straight line segments joining (1,0)-(1,1)-(-1,1)-(-1,0)(b) Straight line segments joining (1,0)-(1,-1)-(-1,-1)-(-1,0):::::20/09/2024:::::E