

CLASS: BTECH
BRANCH: MECHANICAL

SEMESTER : V
SESSION : MO/24

SUBJECT: ME351 FINITE ELEMENT METHODS

TIME: 02 hrs

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- | | | | |
|---|-----|---------|---------|
| Q.1 Obtain an approximate displacement equation by using least squares method for the simply supported beam shown in Figure 1 using the trial solution $y(x)=A\sin(\pi x/H)$. The governing differential equation is | [5] | CO
1 | BL
4 |
|---|-----|---------|---------|

$$EI \frac{d^2 y}{dx^2} - \frac{M_0 x}{H} = 0$$

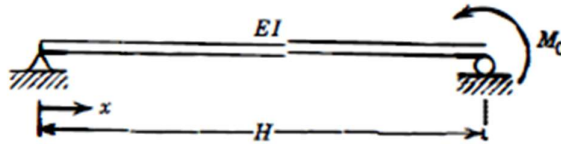


Figure 1

- | | | | |
|--|-----|---|---|
| Q.2 Explain all method for solving boundary value problem. | [3] | 1 | 2 |
|--|-----|---|---|
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- | | | | |
|---|-----|---|---|
| Q.3 The coordinate ξ shown in Figure 2 is a natural coordinate whose origin is at the center of the element. The value of ξ at nodes i and j is 1 and -1, respectively. Develop the shape functions $N_i(\xi)$ and $N_j(\xi)$ starting with $\phi(\xi) = a_1 + a_2 \xi$ and solving for a_1 and a_2 . Also check the shape function is following all the properties | [5] | 2 | 3 |
|---|-----|---|---|

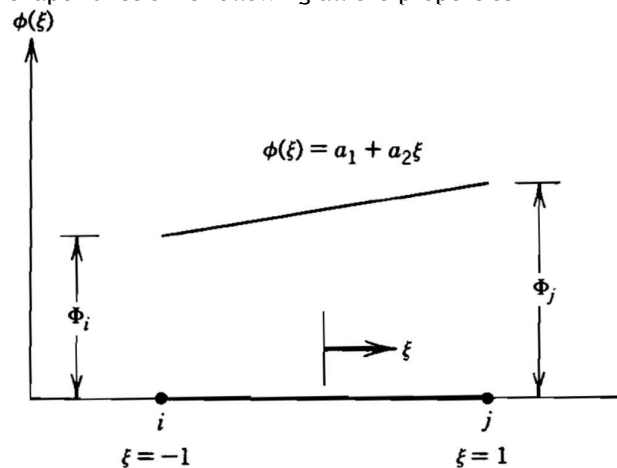


Figure 2

- | | | | |
|--|-----|---|---|
| Q.4 Derive the Galerkin's formulation of nodal residue integrals for the given one dimensional differential equation | [5] | 2 | 3 |
|--|-----|---|---|

$$D \frac{d^2 \phi}{dx^2} + Q = 0$$

Boundary conditions $\phi(0) = \phi_0$ and $\phi(H) = \phi_H$

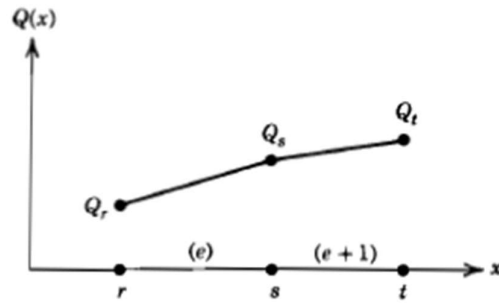
Also Evaluate using linear Elements

Q.5 Evaluate the contribution of

[5] 3 4

$$\int_0^H W Q dx$$

to the Galerkin residual equation R_3 when Q varies linearly over an element



The equation Q in each element is

$$Q^{(e)} = N_r^{(e)} Q_r + N_s^{(e)} Q_s$$

$$Q^{(e+1)} = N_s^{(e+1)} Q_s + N_t^{(e+1)} Q_t$$

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