

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: BTECH
BRANCH: CSE

SEMESTER : III
SESSION : MO/2024

SUBJECT: MA205 DISCRETE MATHEMATICS

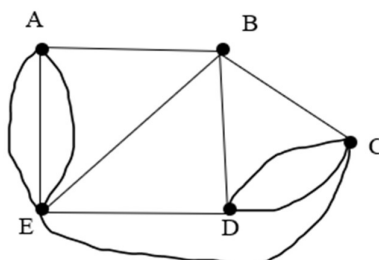
TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Before attempting the question paper, be sure that you have got the correct question paper.
5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

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|--|-----|----|----|
| Q.1(a) Show that $[p \wedge (p \leftrightarrow q)] \rightarrow q$ is a tautology. | [5] | 1 | 3 |
| Q.1(b) Prove that $(p \rightarrow q) \wedge (q \rightarrow r)$ and $(p \vee q) \rightarrow r$ are logically equivalent. | [5] | 1 | 3 |
| Q.2(a) Solve the recurrence relation $a_n = 4a_{n-1} - 4a_{n-2} + 2^n$. | [5] | 2 | 3 |
| Q.2(b) Solve the recurrence relation $a_{n+2} - 2a_{n+1} + a_n = 2^n$ by the method of generating functions with initial conditions $a_0 = 2$ and $a_1 = 1$. | [5] | 2 | 4 |
| Q.3(a) Show that $2x \log(x^2 + 1) = O(x^2)$. | [5] | 3 | 3 |
| Q.3(b) Given $A = \{1, 2, 3, 4\}$ and R is the relation on A represented by the matrix $M_R = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$. Find the transitive closure of R by using Warshall's algorithm. Write W_0, W_1, W_2, W_3 , and W_4 matrices. | [5] | 3 | 4 |
| Q.4(a) Prove that the set $Z_4 = \{0, 1, 2, 3, 4\}$ is an abelian group under the operation addition modulo 5. | [5] | 4 | 3 |
| Q.4(b) Find the minimum distance of the $(2,4)$ encoding function $e: B^2 \rightarrow B^4$ defined by $e(00) = 0000, e(01) = 0110, e(10) = 1011, e(11) = 1100$. | [5] | 4 | 3 |
| Q.5(a) Determine whether the flowing graph is a Euler graph or not. Construct a Euler circuit if it is a Euler graph. | [5] | 5 | 3 |



- Q.5(b) Use Prim's algorithm to find a minimal spanning tree (MST) for the following weighted graph. Find the weight of the MST. [5] 5 4

