

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)**

**CLASS: BTECH
BRANCH: BT/CHEMICAL/ME/PIE/CE/FT**

**SEMESTER : III/ADD
SESSION : MO/2024**

SUBJECT: MA203 NUMERICAL METHODS

TIME: 3 Hours

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Before attempting the question paper, be sure that you have got the correct question paper.
 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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- Q.1(a) Write the Newton Raphson procedure for finding $\sqrt[3]{N}$, where N is a real number. Use it to find $\sqrt[3]{18}$ correct to 2 decimals, assuming $x_0=2.5$. [5]
- Q.1(b) Find the root of the equation $2x - \log_{10} x = 7$ which lies between 3.5 and 4, using method of false Position up to two iterations only. [5]
- Q.2 Perform five iterations of Jacobi iteration method to find the numerical solution of the system of equations: $4x + y + z = 2$; $x + 5y + 2z = -6$; $x + 2y + 3z = -4$ with initial guess: $(1/2, -1/2, -1/2)$. [10]
- Q.3(a) Given that $\sqrt{12500} = 111.8034$, $\sqrt{12510} = 111.8481$, $\sqrt{12520} = 111.8928$, $\sqrt{12500} = 111.9375$, Use Newton Forward difference formula to find $\sqrt{12516}$. [5]
- Q.3(b) Find k in the following table : [5]
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|------|---|---|----|---|-----|
| x | : | 1 | 3 | 4 | 5 |
| f(x) | : | 1 | 25 | k | 121 |
- Q.4 Write the formula of composite Simpson's 1/3 rule with n subintervals. Using this rule, compute the Integral $I = \int_1^2 e^{\{-\frac{x}{2}\}} dx$ with six sub-intervals and find the error with the exact value of the integral. [10]
- Q.5 Using fourth-order Runge-Kutta method find numerical solution of first order initial value problem: $y' = y^2 + x^2$, $y(2) = 3$. Find $y(2.1)$ and $y(2.2)$ by taking $h = 0.1$. [10]

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