BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (MID SEMESTER EXAMINATION MO/2023)

CLASS: B.TECH SEMESTER: V
BRANCH: MECHANICAL SESSION: MO/2023

SUBJECT: ME355 ADVANCED SOLID MECHANICS

TIME: 02 Hours FULL MARKS: 25

INSTRUCTIONS:

- 1. The question paper contains 5 questions each of 5 marks and total 25 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

Q.1 The state of stress at a point is characterised by the components $\sigma_x = 12.31, \ \sigma_y = 8.96, \ \sigma_z = 4.34, \ \tau_{xy} = 4.20, \ \tau_{yz} = 5.27, \ \tau_{zx} = 0.84.$

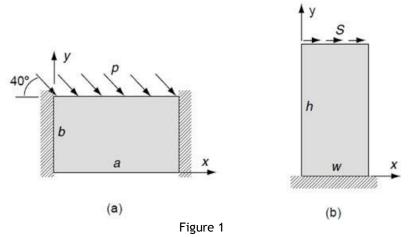
Determine the values of the principal stresses and their directions.

Q.2 The displacement field in suitable units for a body is given by [5] 1 3

$$\vec{u} = (x^2 + y)\hat{i} + (3 + z)\hat{j} + (x^2 + 2y)\hat{k}$$

Determine the principal strains at (3, -1, 2) and the direction of minimum principal strain.

Q.3 Express all boundary conditions for each of the problems illustrated in the Figure 1 [3+2] 1 2 below.



Q.4 A beam-column AB is subjected to an axial load P and a moment M_b at support B as [5] 2 6 shown in Figure 2. Derive the expression of deflection curve of the beam column.



Figure 2

Q.5 Consider a pin-ended column subjected to an axial compressive load P. Assume that ~ [5] ~ 2 ~ 3 the buckled shape of the column is given by $_{\pi \nu}$

$$y = a \sin \frac{\pi x}{L}$$

where \boldsymbol{a} is an unknown parameter. Using the energy method, determine the critical load.