BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (END SEMESTER EXAMINATION)

CLASS: IMSC SEMESTER : III
BRANCH: MATHEMATICS AND COMPUTING SESSION : MO/2023

SUBJECT: MA201 PARTIAL DIFFERENTIAL EQUATION

TIME: 3 Hours FULL MARKS: 50

INSTRUCTIONS:

- 1. The question paper contains 5 questions each of 10 marks and total 50 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Before attempting the question paper, be sure that you have got the correct question paper.
- 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.

| Q.1 | Describe Lagrange's method of finding a solution of a first-order linear partial differential equation. Find a solution of the equation $(y+z)p+(z+x)q=x+y$. | [10] | CO 1 | BL 1.10 1.11 |
|-----|--|------|---------|--------------------|
| Q.2 | Describe the method of finding a solution of a homogeneous linear partial differential equation with constant coefficients. Find a solution to the equation $(D^2-DD^2)z = \cos x$. $\sin 2y$. | [5] | 2 | 1.10 1.12 |
| Q.3 | A tightly stretched flexible string has its end points at $x=0$ and $x=l$. At time $t=0$, the string is given a shape defined by $f(x)=b$ x $(l-x)$, where b is a constant, and then released. Find the displacement of any point x of the string at any time $t>0$. | [10] | 3 | 1.25 1.30 |
| Q.4 | Find the temperature in an infinite bar if the initial temperature is given as $f(x)=U_0$, which is a constant, $ x <1$ and 0 otherwise. | [10] | 4 | 1.25 1.30 |
| Q.5 | Derive a solution of a Dirichlet problem for a rectangle. Boundary conditions may be assumed suitably. | [10] | 5 | 1.31 1.32 |

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