

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI**  
(END SEMESTER EXAMINATION MO/2022)

CLASS: BTECH  
BRANCH: CSE & IT

SEMESTER : III  
SESSION : MO2022

SUBJECT: MA205 DISCRETE MATHEMATICS

TIME: 03 Hours

FULL MARKS: 50

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

Q.1(a) Construct a truth table to determine if the statement  $q \vee (\sim q \wedge p)$  is a tautology, a contingency or an absurdity. (CO1, BT3) [2]

Q.1(b) Show that  $k$  is odd if and only if  $k^3$  is odd. (CO4, BT3) [3]

Q.1(c) Use mathematical induction to prove that  $1 + 2 + 3 + \dots + n < \frac{(n+1)^2}{2}$  (CO4, BT3) [5]

Q.2(a) Solve the recurrence relation  $b_n = -3b_n - 2b_{n-2}$ ,  $b_1 = -2$ ;  $b_2 = 4$  (CO1, BT3) [2]

Q.2(b) Find the particular solution of the recurrence relation  $a_r + 5a_{r-1} + 6a_{r-2} = 3r^2$  (CO1, BT1) [3]

Q.2(c) Solve the recurrence  $a_{r+2} - 5a_{r+1} + 6a_r = 2$  by the method of generating function satisfying the initial conditions  $a_0 = 1$  and  $a_1 = 3$ . (CO4, BT1) [5]

Q.3(a) Let  $A = \{1,2,3\}$  and  $R = \{(1,2), (2,3), (2,1)\}$ . Find the transitive closure of R. (CO2, BT4) [2]

Q.3(b) Give a big-O estimate of  $f(n) = 3n \log n! + (n^2 + 3)$  (CO5, BT2) [3]

Q.3(c) [5]

Let  $A = \{1,2,3,4\}$  and R is the relation whose matrix is  $M_R = \begin{bmatrix} 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \end{bmatrix}$

Determine whether R is reflexive, irreflexive, symmetric, asymmetric, antisymmetric or transitive. Give reasons for your answer. (CO5, BT5)

Q.4(a) Let  $A = \mathbb{Z}^+$  and R be the relation on A defined by  $aRb$  iff  $b = a+1$ . Give the transitive closure of R. (CO5, BT5) [2]

Q.4(b) [3]

Let  $H = \begin{bmatrix} 0 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

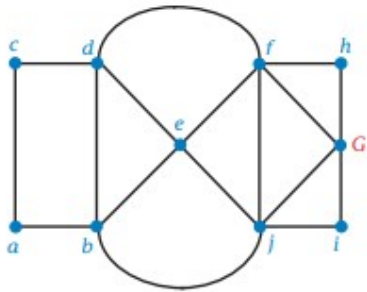
be a parity check matrix. Determine the (3,6) group code  $e_H : B^3 \rightarrow B^6$ .

(CO2, BT5)

Q.4(c)  $f = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 2 & 1 \end{bmatrix}$ ,  $g = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 1 & 2 \end{bmatrix}$ ,  $h = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 3 \end{bmatrix}$ . Find whether f and g are commutative or not [5]

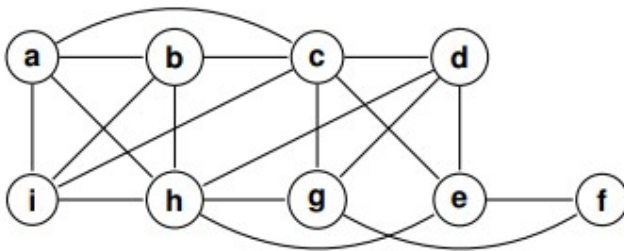
under composition. Find whether f, g and h follow the associative law or not. (CO5, BT1)

Q.5(a) If possible find Hamiltonian circuit of following graph. [2]



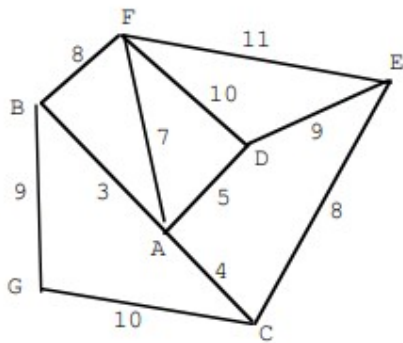
(CO2, BT4)

Q.5(b) Determine whether the given graph has an Euler circuit and construct such a circuit by Fleury's algorithm when one exists. [3]



(CO5 , BT5)

Q.5(c) Find minimum cost spanning tree by Prim's algorithm [5]



(CO2, BT6)