

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(END SEMESTER EXAMINATION)

CLASS: IMSc.  
BRANCH: QEDS

SEMESTER : I  
SESSION : MO/2022

SUBJECT: ED107 PROBABILITY - I

TIME: 3 Hours

FULL MARKS: 50

**INSTRUCTIONS:**

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
  2. Attempt all questions.
  3. The missing data, if any, may be assumed suitably.
  4. Before attempting the question paper, be sure that you have got the correct question paper.
  5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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		CO	BL
Q.1(a)	A college planning committee consists of 3 freshmen, 4 sophomores, 5 juniors and 2 seniors. A subcommittee of 4, consisting of 1 person from each class is to be chosen. How many different subcommittees are possible?	[5]	1
Q.1(b)	Ten children are divided into an A team and a B team of 5 each. How many different divisions are possible?	[5]	1
Q.2(a)	An insurance company believes that an accident-prone person will have an accident at some time within a fixed 1-year period with probability 0.4, whereas this probability decreases to 0.2 for a non-accident-prone person. If we assume that 30% of the population is accident-prone, what is the probability that a new policy holder will have accident within a year of purchasing policy?	[5]	2
Q.2(b)	Suppose that a new policy holder has an accident within a year of purchasing a policy. What is the probability that he or she is accident prone?	[5]	2
Q.3(a)	Three balls are chosen randomly from an urn containing 3 white, 3 red and 5 black balls. We win \$1 for each white ball selected and lose \$1 for each red ball selected. If X denote the total winnings from the experiment find the probability distribution of X.	[5]	3
Q.3(b)	Find E(X) and V(X) where X is the outcome when we roll a fair die.	[5]	3
Q.4(a)	The amount of time, in hours, that a computer functions before breaking down is a random variable with pdf $f(x) = \lambda e^{-x/100}$ , $x > 0$ , and 0, otherwise. What is the probability that a computer will function between 50 and 150 hours before breaking down?	[5]	4
Q.4(b)	It will function less than 100 hours?	[5]	4
Q.5	Suppose that 3 balls are randomly selected from an urn containing 3 red, 4 white, and 5 blue balls. If X and Y denote, respectively, the number of red and white balls chosen, find the joint probability mass function of X and Y. Check for the independence of the random variables.	[10]	5

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