

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI  
(MID SEMESTER EXAMINATION MO 2022)

CLASS: IMSC  
BRANCH: QEDS

SEMESTER : I  
SESSION: MO2022

TIME: 02 HOURS

SUBJECT: ED101 INTRODUCTORY ANALYSIS

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
  2. Attempt all questions.
  3. The missing data, if any, may be assumed suitably.
  4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates
- 

- Q1 a. Is the set of all the prime numbers in  $[1,100]$  an open set? Justify your answer. [2] CO BL  
b. Define uncountable set. Give an example of an uncountable set. Justify your answer. [3] CO1
- Q2 a. Find the supremum, infimum, greatest element and least element, if exist, of the set  $S = \{x \in \mathbb{R} | x^2 \geq 3x + 10\}$ . [3] CO1  
b. Prove that  $\sqrt{10}$  is an irrational number. [2] CO1
- Q3 a. State and prove Cauchy's general principle for the convergence of a sequence of real numbers. [3] CO2  
b. Check the convergency of the sequence  $\{S_n\}$ , where [2] CO2  
$$S_n = 1 + \frac{1}{4} + \frac{1}{7} + \dots + \frac{1}{3n-2}$$
by Cauchy's general principle for convergence.
- Q4 a. Show that the sequence  $\{x_n\}$ , defined by [3] CO2  
 $x_1 = 1, x_{n+1} = \sqrt{5x_n}, n > 1$   
converges to 5.  
b. Check whether the alternating series  $\sum_{n=2}^{\infty} (-1)^{n-1} \frac{1}{(n-1)^4}$  is absolute [2] CO2  
convergent  
or conditional convergent.
- Q5 Test for the convergency of the infinite series [5] CO2  
$$1 + \frac{3}{7}x + \frac{3.6}{7.10}x^2 + \frac{3.6.9}{7.10.13}x^3 + \dots, x > 0.$$

:::::16/01/2023:::::M