

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)**

**CLASS: BE
BRANCH: ECE**

**SEMESTER : VII
SESSION : MO/19**

SUBJECT: MEC1125 INFORMATION THEORY AND CODING

TIME: 3:00 HOURS

FULL MARKS: 60

INSTRUCTIONS:

1. The question paper contains 7 questions each of 12 marks and total 84 marks.
 2. Candidates may attempt any 5 questions maximum of 60 marks.
 3. The missing data, if any, may be assumed suitably.
 4. Before attempting the question paper, be sure that you have got the correct question paper.
 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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- Q.1(a) Define Kullback-Leibler distance between two probability mass functions. [2]
- Q.1(b) Explain, entropy is a concave function. [4]
- Q.1(c) Prove that the entropy of a Gaussian random variable is only depending upon its finite variance of the distribution. Also compare its entropy with other continuous random variables. [6]
- Q.2(a) Define Instantaneous Codes. [2]
- Q.2(b) Consider a discrete memoryless source having alphabet $\mathcal{Y} = \{A_1, A_2, A_3, A_4\}$ and corresponding probabilities $\{0.5, 0.125, 0.25, \text{ and } 0.125\}$. Determine the arithmetic code for the sequence $A_2A_3A_1A_4A_1$ with pictorial illustration. [4]
- Q.2(c) Describe Huffman coding algorithm. Consider a DMS with probabilities 0.37, 0.33, 0.16, 0.07, 0.04, 0.02 and 0.01, respectively. Construct Huffman coding for the DMS and find out code efficiency. [6]
- Q.3(a) Describe the basic properties of Binary Symmetric Channel and Binary Erasure Channel. [2]
- Q.3(b) Evaluate the overall channel capacity of two cascaded connected BSC channels assuming that all have the same transition probability diagram with $p=0.2$ [4]
- Q.3(c) Prove that the information capacity of a continuous channel of bandwidth W hertz, perturbed by additive Gaussian noise of power spectral density $N_0/2$ is given by $C = W \log_2 \left(1 + \frac{P}{N_0 W} \right)$ bits/sec. [6]
- Q.4(a) What is systematic encoder? [2]
- Q.4(b) Explain the Singleton and the Humming bounds for linear block codes. [4]
- Q.4(c) Consider a $(n, k) = (7, 1)$ repetition code generated by the generator matrix $G = [1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$. Evaluate the syndrome S for all possible single-error patterns. [6]
- Q.5(a) Define primitive element of a Galois field. [2]
- Q.5(b) Explain BCH code. [4]
- Q.5(c) For nonsystematic coding in $(7, 3)$ cyclic code (under $GF(2)$) with generator polynomial $g(x) = (1+x)(x^3+x+1)$, determine generator matrix, G & parity check matrix, H . [6]
- Q.6(a) Define code rate and constraint length of a convolutional encoder. [2]
- Q.6(b) Draw convolutional encoder, state diagram and its one stage of trellis diagram with transfer function matrix $G(x) = [1+x^2 \ x+x^2]$. [4]
- Q.6(c) Describe Viterbi decoding of convolutional codes with its advantages. [6]
- Q.7(a) What is the difference between Block cipher and Stream cipher? [2]
- Q.7(b) Explain public-key encryption using block diagram. How can we incorporate authentication using the digital signature? [4]
- Q.7(c) Discuss RSA algorithm with suitable example. [6]

:29/11/2019: