

**BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)**

**CLASS: MCA
BRANCH: MCA**

**SEMESTER : V
SESSION : MO/18**

SUBJECT: MCA5005 OPTIMIZATION THEORY

TIME: 3 HRS.

FULL MARKS: 60

INSTRUCTIONS:

1. The question paper contains 7 questions each of 12 marks and total 84 marks.
 2. Candidates may attempt any 5 questions maximum of 60 marks.
 3. The missing data, if any, may be assumed suitably.
 4. Before attempting the question paper, be sure that you have got the correct question paper.
 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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- Q.1(a) Describe the phases of Operation Research. [6]
- Q.1(b) Consider the example of a manufacturer of animal feed who is producing feed mix for dairy cattle. [6]
In our simple example the feed mix contains two active ingredients and a filler to provide bulk.
One kg of feed mix must contain a minimum quantity of each of four nutrients as below:
Nutrient A B C D
gram 90 50 20 2
The ingredients have the following nutrient values and cost

	A	B	C	D	Cost/kg
Ingredient 1 (gram/kg)	100	80	40	10	40
Ingredient 2 (gram/kg)	200	150	20	-	60

What should be the amounts of active ingredients and filler in one kg of feed mix?
- Q.2(a) Differentiate in following: [2+2+2+]
(i) infeasible and unbounded (show graphically)
(ii) Constraints and basic variables
(iii) Optimal and feasible solution
- Q.2(b) For an optimization problem following facts are given [6]
■ Hot dog mixture in 1000-pound batches.
■ Two ingredients, chicken (\$3/lb) and beef (\$5/lb).
■ Recipe requirements:
 at least 500 pounds of "chicken"
 at least 200 pounds of "beef"
■ Ratio of chicken to beef must be at least 2 to 1.
■ Determine optimal mixture of ingredients that will minimize costs. Solve it graphically.
- Q.3(a) Solve following LPP using simplex method [6]
Max $Z = x + 1.2y$
s.t. $2x + y \leq 180$
 $x + 3y \leq 300$
 $x, y \geq 0$
- Q.3(b) Explain BIG-M method with example. [6]
- Q.4(a) Show that dual of given LPP has no variables is same as no of constraints in primal. [4]
Min $Z_x = x_1 - 3x_2 - 2x_3$
s.t. $3x_1 - x_2 + 2x_3 \leq 7$
 $2x_1 - 4x_2 \geq 12$
 $-4x_1 + 3x_2 + 8x_3 = 10$
And $x_1, x_2 \geq 0$, x_3 is unrestricted
- Q.4(b) Solve given LPP by dual simplex method [8]
Min $z = 2x_1 + x_2$
s.t. $3x_1 + 2x_2 \geq 3$
 $2x_1 + 3x_2 \geq 6$
 $3x_1 + 2x_2 \leq 3$
 $x_i \geq 0$

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- Q.5(a) Differentiate between pure integer programming and mixed integer programming. [4]
 Q.5(b) Solve given LPP by revised simplex method [8]

Max $Z=2x+y$
 s. t. $3x+4y \leq 6$
 $6x+y \leq 3$
 And $x, y \geq 0$

- Q.6 Find minimum path using dynamic programming for given stage coach problem. [12]

	B	C	D
A	2	4	3

	E	F	G
B	8	7	5
C	3	2	4
D	4	1	5

	H	I
E	9	3
F	7	5
G	9	4

	J
H	3
I	8

- Q.7(a) What is Quadratic programming? [6]
 Q.7(b) What is separable convex programming problem and how they are different then quadratic programming? [6]

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