

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(END SEMESTER EXAMINATION)

CLASS: M.TECH
BRANCH: IT

SEMESTER : I
SESSION : MO/18

SUBJECT: IT501 INFORMATION AND CODING THEORY

TIME: 3 HOURS

FULL MARKS: 50

INSTRUCTIONS:

1. The question paper contains 5 questions each of 10 marks and total 50 marks.
 2. Attempt all questions.
 3. The missing data, if any, may be assumed suitably.
 4. Before attempting the question paper, be sure that you have got the correct question paper.
 5. Tables/Data hand book/Graph paper etc. to be supplied to the candidates in the examination hall.
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- Q.1(a) Explain mutual information average conditional self-information and entropy. Give examples for each. [4]
- Q.1(b) Consider a DMS with eight possible symbols $x_i, i=1, \dots, 8$ and the corresponding probabilities $p_1=0.34, p_2=0.12, p_3=0.07, p_4=0.29, p_5=0.02, p_6=0.01, p_7=0.11$ and $p_8=0.04$. Find the code words using Huffman coding technique. Also find $H(X)$ and R . [6]
- Q.2(a) State and explain channel coding theorem. [6]
- Q.2(b) Show that for reliable communication $C \leq I$ where I and C have their own meaning. [4]
- Q.3(a) Find the linear span of $S = \{12, 21\}$ defined over $GF(3)$ [3]
- Q.3(b) Explain parity check matrix in case of linear block code. [3]
- Q.3(c) Find a (5,2) systematic code over $GF(3)$. [4]
- Q.4(a) Consider the ring $F[x]/(x^2+1)$ defined over $GF(2)$. Is it a field? Justify your answer. [3]
- Q.4(b) Find the generator matrices of the codes (4,4) and (4,3) of all codes defined over $GF(3)$ of block length $n=4$. [3]
- Q.4(c) Let us consider all binary codes of block length 7. Find the matrix H corresponding to $\log(x) = x^3 + x^2 + 1$. [4]
- Q.5(a) Find the addition table of the Galois field $GF(2^3)$ and Find $\alpha^5 + \alpha + 1$. [3]
- Q.5(b) Show that α^3 in $GF(2^4)$ is not a primitive element. [3]
- Q.5(c) Construct a double-error-correcting BCH code over $GF(2^4)$. [4]

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