# BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI <br> (END SEMESTER EXAMINATION) 

CLASS: B PHARMACY
SEMESTER: I
BRANCH: PHARM SCI TECH
SUBJECT: BP106RMT REMEDIAL MATHEMATICS
TIME: 1.30 Hour
FULL MARK: 35
A. Short Answers
(Answer five out of seven)
(05×05 = 25 marks)

1. Define Proper Fraction and resolve into partial fraction: $\frac{x}{(x+1)^{2}(x-3)}$.
2. If $x$ and $y$ are real number such that, $2 \log (2 y-3 x)=\log x+\log y$, find $\frac{y}{x}$.
3. Show that, $\left|\begin{array}{lll}a & b & c \\ b & c & a \\ c & a & b\end{array}\right|=-\left(a^{3}+b^{3}+c^{3}-3 a b c\right)$.
4. Find the maximum and minimum value of the function $x^{3}-3 x^{2}+3 x-11=0$.
5. Evaluate the integrals: (a.) $\int \sqrt{a x+b} d x \quad$ (b.) $\int_{0}^{\frac{\pi}{2}} \sin ^{3} x \cos x d x$
6. Define Order and Degree. Find the order and degree of the following differential equation.
(a.) $\frac{d^{2} y}{d x^{2}}+5\left(\frac{d y}{d x}\right)^{2}+2 y=0$
(b.) $\sqrt{1+\left(\frac{d y}{d x}\right)^{2}}=1+x$.
7. Solve the homogeneous differential equation, $\frac{d y}{d x}=\frac{x+2 y}{2 x-y}$.
B. Long Answers
(Answer one out of two) (01 $\times 10=10$ marks)
8. If $(x)=x+\frac{1}{x-2}+e^{-x}$, then find the value of following.
(a.) $f(0), f(1)$
(b.) $\lim _{x \rightarrow 0} f(x)$
(c.) $\frac{d f}{d x}$ and $\frac{d f}{d x}$ at $x=0$.
(d.) $\int f(x) d x$ and $\int_{0}^{1} f(x) d x$.
9. Consider the system of equations, $x-2 y+2 z=2 ; 2 x-y-2 z=1 ; 2 x+2 y+z=7$.
(a.) Write the system of equation in the form of $A X=B$.
(b.) Find the inverse of the matrix A.
(c.) Find the Eigen value of A.
